

1. Prove that for any natural numbers  $n$  and  $d$  there are unique  $q$  and  $r$  such that  $n = q \cdot d + r$  where  $-d \leq r < 0$ .
2. Prove for  $n \geq 4$  that  $n^3 + 20 > n^2 + 15n$ .
3. Prove that  $\sum_{i=1}^n i(i+1) = \frac{n(n+1)(n+2)}{3}$ .
4. For  $n \in \mathbb{N}$  prove that if  $x < y$  then  $x^{2n-1} < y^{2n-1}$ .